ORDER OF OPERATIONS

The first step is to organize the numerical expression into parts called terms, which are single numbers or products of numbers. A numerical expression is made up of a sum or difference of terms.

Examples of numerical terms are: 4, 3(6), 6(9 – 4), $2 \cdot 3^2$, 3(5 + 2^3), and $\frac{16-4}{6}$.

For the problem above, $3 + 4 \cdot 2$, the terms are circled at right.

$$(3) + (4 \cdot 2)$$

Each term is simplified separately, giving 3 + 8. Then the terms are added: 3 + 8 = 11. Thus, $3 + 4 \cdot 2 = 11$.

Example 1

To evaluate an expression:

- Circle each term in the expression.
- Simplify each term until it is one number by:
 Simplifying the expressions within the parentheses.

 Evaluating each exponential part (e.g., 3²).
 Multiplying and dividing from left to right.
- Finally, combine terms by adding or subtracting from left to right.

$$2 \cdot 3^2 + 3(6-3) + 10$$

- $(2 \cdot 3^2) + (6 3) + (10)$
- $(2 \cdot 3^2) + (3(3)) + (10)$
- $2 \cdot 9 + 3(3) + 10$
 - 18 + 9 + 10

27 + 10 37

Example 2

- a. Circle the terms.
- b. Simplify inside the parentheses.
- c. Simplify the exponents.
- d. Multiply and divide from left to right.

Finally, add and subtract from left to right.

$$5-8 \div 2^2 + 6(5+4) - 5^2$$

- a. $(5)-(8 \div 2^2)+(6(5+4))-(5^2)$
- b. (5) $-(8 \div 2^2)$ +(6(9)) $-(5^2)$
- c. $(5)-(8\div4)+(6(9))-(25)$
- d. 5-2+54-25

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Example 3

 $20 + \frac{5+7}{3} - 4^2 + 12 \div 4$

a. Circle the terms.

- b. Multiply and divide left to right, including exponents.
- 20 + 4 16 + 3b.

Add or subtract from left to right.

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Problems

Circle the terms, then simplify each expression.

1.
$$5 \cdot 3 + 4$$

2.
$$10 \div 5 + 3$$

3.
$$2(9-4)\cdot 7$$

4.
$$6(7+3)+8 \div 2$$

5.
$$15 \div 3 + 7(8 + 1) - 6$$

4.
$$6(7+3)+8 \div 2$$
 5. $15 \div 3+7(8+1)-6$ 6. $\frac{9}{3}+5\cdot 3^2-2(14-5)$

7.
$$\frac{20}{6+4} + 7 \cdot 2 \div 2$$

7.
$$\frac{20}{6+4} + 7 \cdot 2 \div 2$$
 8. $\frac{5+30}{7} + 6^2 - 18 \div 9$ 9. $2^3 + 8 - 16 \div 8 \cdot 2$

9.
$$2^3 + 8 - 16 \div 8 \cdot 2$$

10.
$$25-5^2+9-3^2$$

10.
$$25-5^2+9-3^2$$
 11. $5(17-7)+4\cdot 3-8$ 12. $(5-2)^2+(9+1)^2$

12.
$$(5-2)^2 + (9+1)^2$$

13.
$$4^2 + 9(2) \div 6 + (6-1)^2$$
 14. $\frac{18}{3^2} + \frac{5 \cdot 3}{5}$ 15. $3(7-2)^2 + 8 \div 4 - 6 \cdot 5$

14.
$$\frac{18}{3^2} + \frac{5.3}{5}$$

15.
$$3(7-2)^2 + 8 \div 4 - 6 \cdot 5$$

16.
$$14 \div 2 + 6 \cdot 8 \div 2 - (9 - 3)$$

16.
$$14 \div 2 + 6 \cdot 8 \div 2 - (9 - 3)^2$$
 17. $\frac{27}{3} + 18 - 9 \div 3 - (3 + 4)^2$

18.
$$26 \cdot 2 \div 4 - (6+4)^2 + 3(5-2)^3$$
 19. $\left(\frac{42+3}{5}\right)^2 + 3^2 - \left(5 \cdot 2\right)^2$

19.
$$\left(\frac{42+3}{5}\right)^2 + 3^2 - (5\cdot 2)^2$$

Answers

1. 19

2. 5

3. 70

4. 64

5. 62

6. 30

7. 9

8. 39

9. 12

10. 0

11. 54

12. 109

13. 44

14. 5

15. 47

16. –5

17. –25

18. -6

19. -10